

**2.14** Using two linear elements solve the equations in problem (2.13) with  $L = 1 \text{ m}$ ,  $K = 200 \text{ W/mK}$ ,  $Q = 100 \text{ W/m}^3$ ,  $h = 150 \text{ W/m}^2 \text{ K}$ ,  $T_\infty = 100^\circ\text{C}$  and  $q = 2,000 \text{ W/m}^2$ .

**Solution:**

Using Eqs. 2.19 and 2.30  $\frac{2K}{L} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \begin{Bmatrix} T_1 \\ T_2 \end{Bmatrix} - \frac{QL}{4} \begin{Bmatrix} 1 \\ 1 \end{Bmatrix} - h \begin{Bmatrix} T_1 - T_\infty \\ 0 \end{Bmatrix} = \begin{Bmatrix} 0 \\ 0 \end{Bmatrix}$  Substitute the

parameters values 1)  $\begin{bmatrix} 250 & -400 \\ -400 & 400 \end{bmatrix} \begin{Bmatrix} T_1 \\ T_2 \end{Bmatrix} = \begin{Bmatrix} -14750 \\ 25 \end{Bmatrix}$  2)  $\begin{bmatrix} 400 & -400 \\ -400 & 400 \end{bmatrix} \begin{Bmatrix} T_2 \\ T_3 \end{Bmatrix} = \begin{Bmatrix} 25 \\ 25 - q \end{Bmatrix}$

assembling

$$1) \begin{bmatrix} 250 & -400 & 0 \\ -400 & 800 & -400 \\ 0 & -400 & 400 \end{bmatrix} \begin{Bmatrix} T_1 \\ T_2 \\ T_3 \end{Bmatrix} = \begin{Bmatrix} -14750 \\ 50 \\ 25 - q \end{Bmatrix} \quad \text{With solution} \quad \begin{aligned} T_1 &= 97.833 + 0.0066667q \\ T_2 &= 98.021 + 0.0041667q \\ T_3 &= 98.084 + 0.0016667q \end{aligned}$$